



# Longitudinal Dynamics in the Stanford Linear Collider Damping Rings

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*BNL*



# Outline

- Introduction  
*SLC, Damping Rings, BPM signals, Instability history*
- Hardware  
*BPM signal processing, Streak camera, Control system interface*
- Experimental studies at high current  
*Instability phase space structure, Linac correlation studies, Stored beam studies*
- Impedance-related measurements  
*Synchronous phase measurement, Low current streak camera measurements, Tune shifts with current*
- Conclusion



# Parameters for the SLC Damping Rings Related to Longitudinal Dynamics and Diagnostics

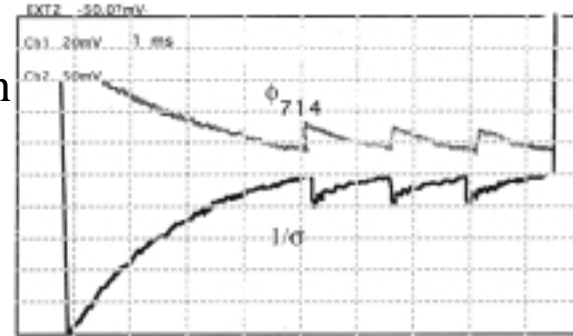
| Parameter                              | Symbol                  | Value                                |
|--|-------------------------|--------------------------------------|
| Energy                                 | $E_0$                   | 1.19 GeV                             |
| Typical Population per bunch           | $N$                     | $4.5 \times 10^{10}$                 |
| Number of bunches                      |                         | 2                                    |
| Store time (NDR, SDR)                  |                         | 8.3 ms, 16.6 ms                      |
| Orbit Circumference                    | $C$                     | 35.27 m                              |
| Revolution Frequency                   | $f_0, \omega_0/2\pi$    | 8.5 MHz                              |
| RF Frequency                           | $f_{RF}$                | 714 MHz                              |
| Harmonic Number                        | $h$                     | 84                                   |
| Typical RF Voltage                     | $V_{RF}$                | 800 kV                               |
| Typical Synchrotron Frequency          | $f_s, \omega_s/2\pi$    | 100 kHz                              |
| Energy Spread (in, out)                | $\delta_{inj}, \delta$  | $3 \times 10^{-3}, 9 \times 10^{-4}$ |
| Bunch Length (in, out)                 | $\sigma_{inj}, \sigma$  | 7.4 ps, 20-25 ps                     |
| Zero Current Bunch Length              | $\sigma_0$              | 17.8 ps                              |
| Energy Loss/turn from Synch. Radiation | $U_0$                   | 79.2 KeV                             |
| Momentum Compaction                    | $\alpha$                | 0.015                                |
| Energy Damping Time (NDR, SDR)         | $\tau_d, \gamma_d^{-1}$ | 1.91 ms, 1.78 ms                     |

$$\frac{Nr_0}{\delta_0^2 \alpha \gamma C} \frac{4\pi |Z_{||\text{eff}}|}{Z_0} \sim 6$$

*Strong Longitudinal Single Bunch Effects Expected!*

# Instability History

- 1992
  - Attempt to raise current above  $3 \times 10^{10}$ /bunch*
  - Severe single bunch longitudinal instability*
  - Transient, “Saw-tooth” behavior*
  - Inability to operate the linac*

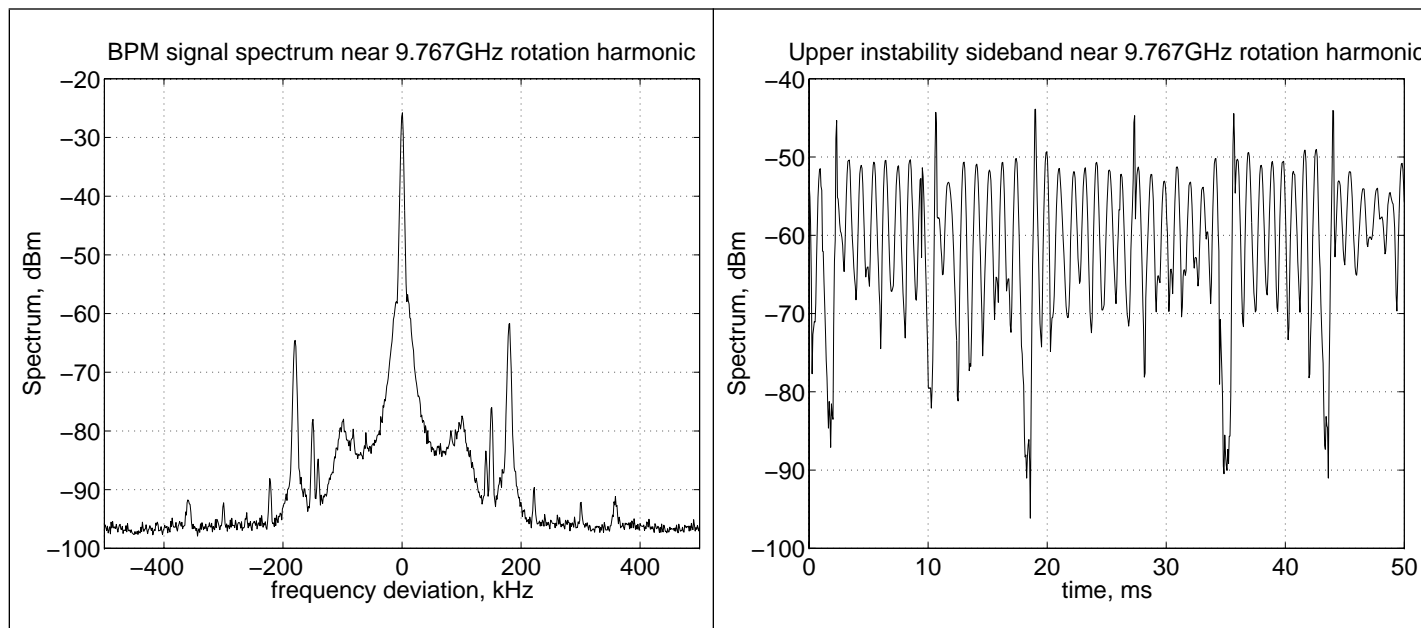


*P. Krejcik et. al., PAC-93*

- 1993
  - Solution - vacuum chamber replacement. Total inductance was reduced by a factor of 5.*
  - Simulations predicted threshold of  $5 \times 10^{10}$ /bunch*
- 1994-1998
  - The actual threshold went down  $\sim 2 \times 10^{10}$ /bunch*
  - Instability less severe. Saturates at lower level. It is no longer the main limiting factor for the SLC*

# “New Saw-Tooth” Instability

## BPM Signals on a Spectrum Analyzer



### *Other Measurements*

- Wire scanner - energy spread growth above the threshold
- Streak Camera - no signs of instability other than bunch lengthening
- No measurable effect on the linac

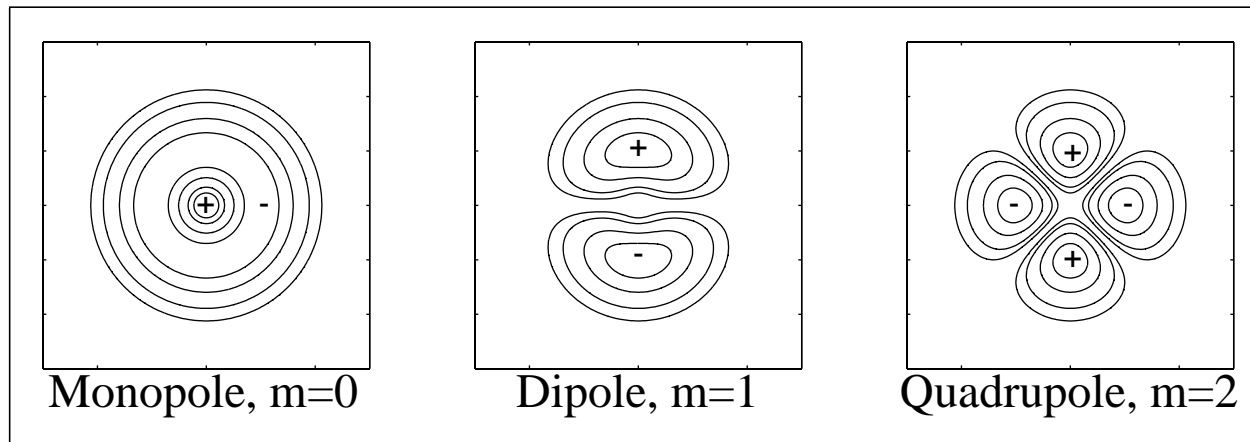
*Something had to be there -> Need for new hardware*

# Collective Modes in Longitudinal Phase Space

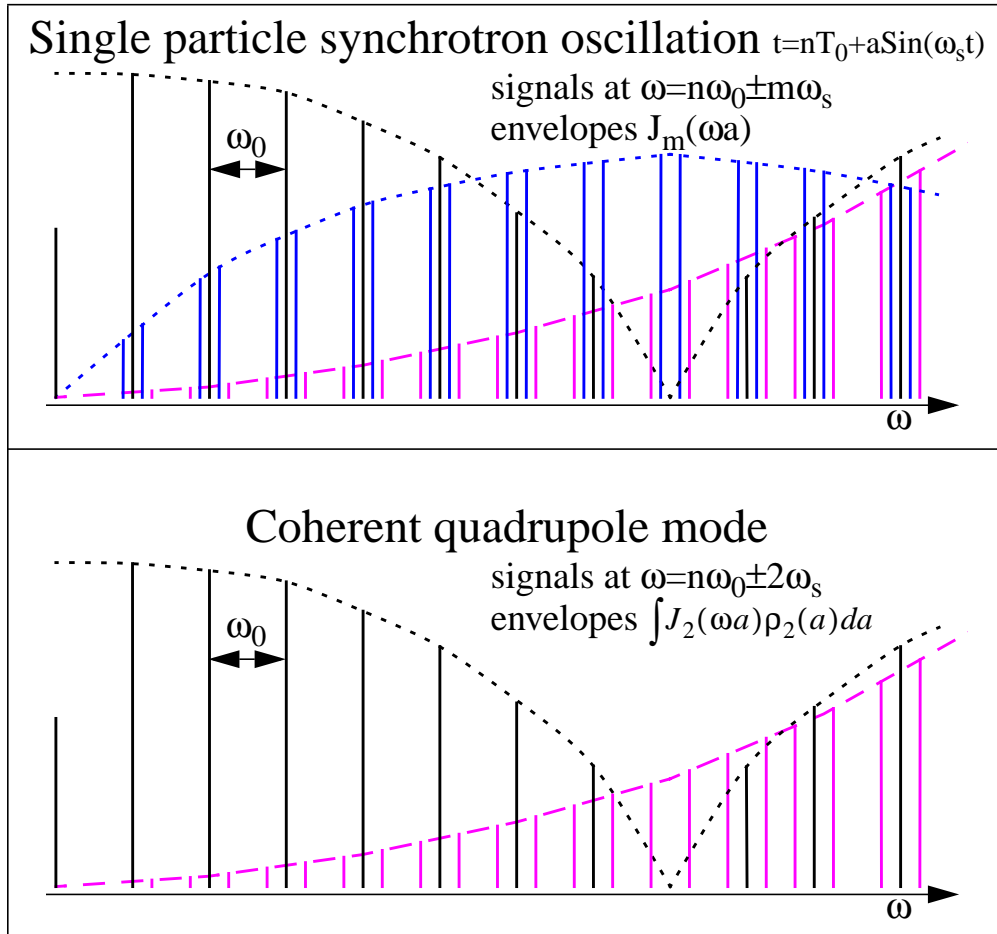
- Canonical coordinates  $x \equiv \frac{z}{\sigma_0}$ ,  $p \equiv -\frac{\delta}{\delta_0}$ , time normalized to synchrotron period  $\tau \equiv \omega_{s0}t$ , index denotes zero current
- Action-angle variables (usually from the steady state Haissinski solution)  $\rho_H(p, x) \Rightarrow \rho_H(J)$
- In the limit of low intensity  $J \rightarrow \frac{p^2}{2} + \frac{x^2}{2}$ ,  $\phi \rightarrow \text{asin}\left(\frac{p}{x}\right)$
- Beam phase space density is Fourier transformed into sum over azimuthal modes

$$\rho(J, \phi, t) = \sum_m \rho_m(J) e^{i\Omega\tau - im\phi}$$

Example of the first three azimuthal modes



# BPM Signal Spectra and Longitudinal Phase Space



- m-th sideband suggests collective mode with m-fold azimuthal symmetry
- Need to go to high frequency  $\omega \sim m/\sigma$
- Spectrum completely describes beam phase space
- Radial structure is in the envelope
- Azimuthal orientation is in phase of any sideband



## Experimental Goals

*of our studies was to answer the questions*

- What was the effect of the instability on the beam?
- What was the effect (if any) on the SLC performance?





## Problems with Old Hardware

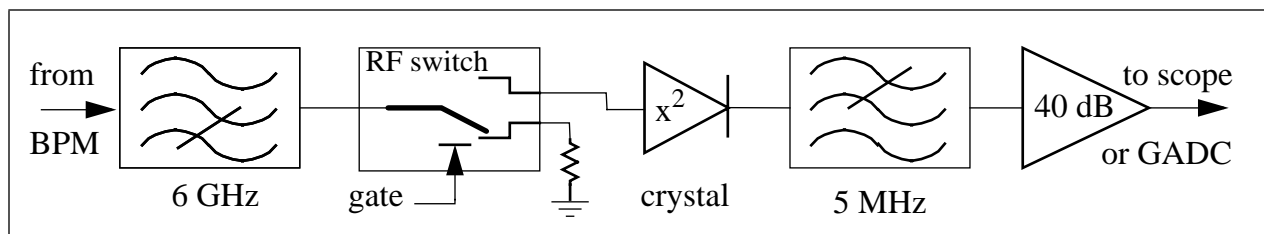
- Most instruments (wire scanner, streak camera) allowed only integrated measurements averaged over many injection cycles
- Spectrum analyzer shows instability presence within one injection cycle but not much else. It does not measure phase
- Studies of a single bunch instability require BPM signal from a single bunch
- Linac correlation studies require differentiation between bunches and stores

## Ideas for New Apparatus

- We can distinguish two bunches employing fast RF switch
- Instability information resides mainly in sidebands to high frequency revolution harmonics. It can be demodulated from those sidebands
- Low frequency (less than a few GHz) BPM signal is not useful and too high in amplitude. It should be filtered out

# Detecting Instability Signal I

## Detector Schematics



Cuts RF power

Separates two bunches

Detects instability signal

Removes higher frequency products

*Switch is gated at revolution frequency of 8.5 MHz and gate delay is adjusted to separate two bunches*

## RF Switch and Crystal Specifications

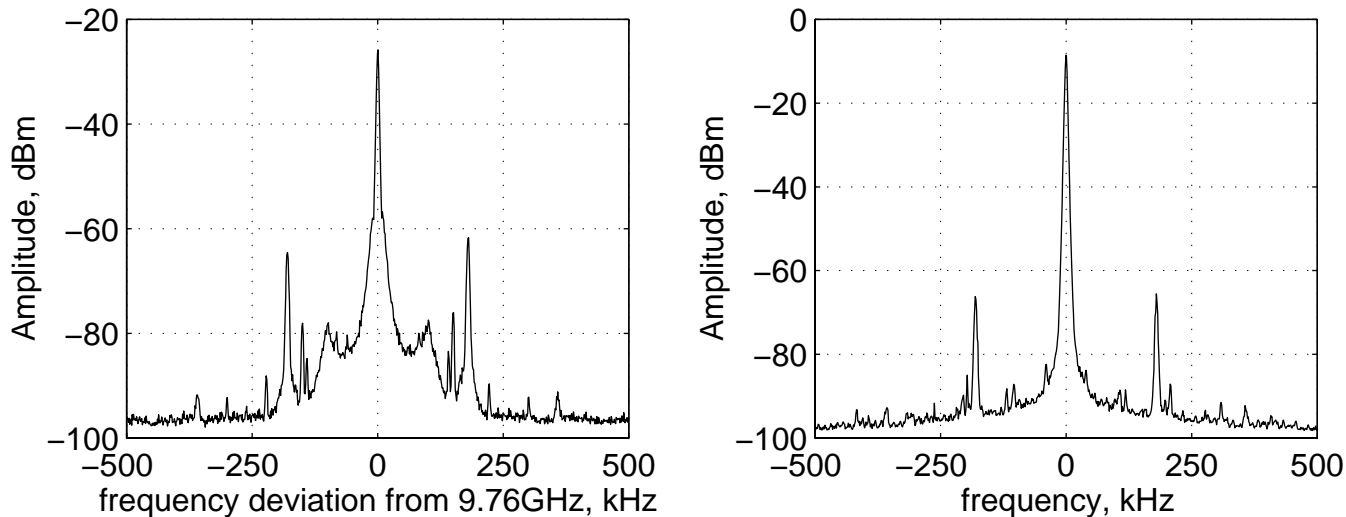
|                 | WJ-MSE203       | MITEQ-S138B     | ACTP-1506N          |
|-----------------|-----------------|-----------------|---------------------|
| Type            | SPDT Reflective | SPST Absorptive | Square Law Detector |
| Bandwidth       | 2-18 GHz        | 2-18 GHz        | 8-18 GHz            |
| Switching time  | 25 ns           | 20 ns           | N/A                 |
| Isolation       | ~60 dB          | 80 dB           | N/A                 |
| Video Bandwidth | N/A             | N/A             | 2 MHz               |

### Detector

- provides single bunch “instability signal”
- the phase of this signal relates to the azimuthal orientation of the instability-induced phase space structure

# Detecting Instability Signal II

Spectrum Analyzer Traces before and after the Crystal



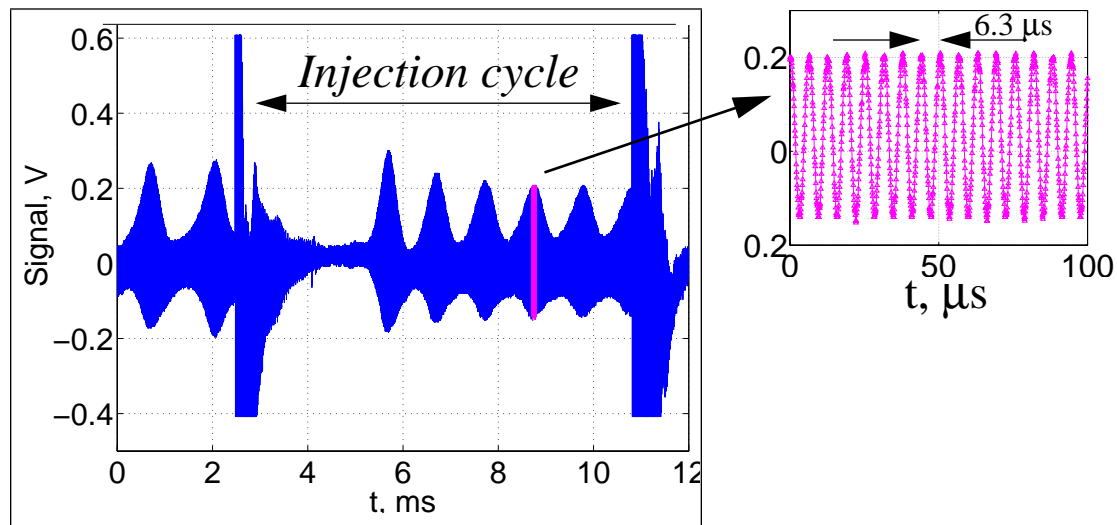
Signal after the Detecting Circuit

*Instability frequency*

$$160 \text{ kHz} \sim 2 f_s$$

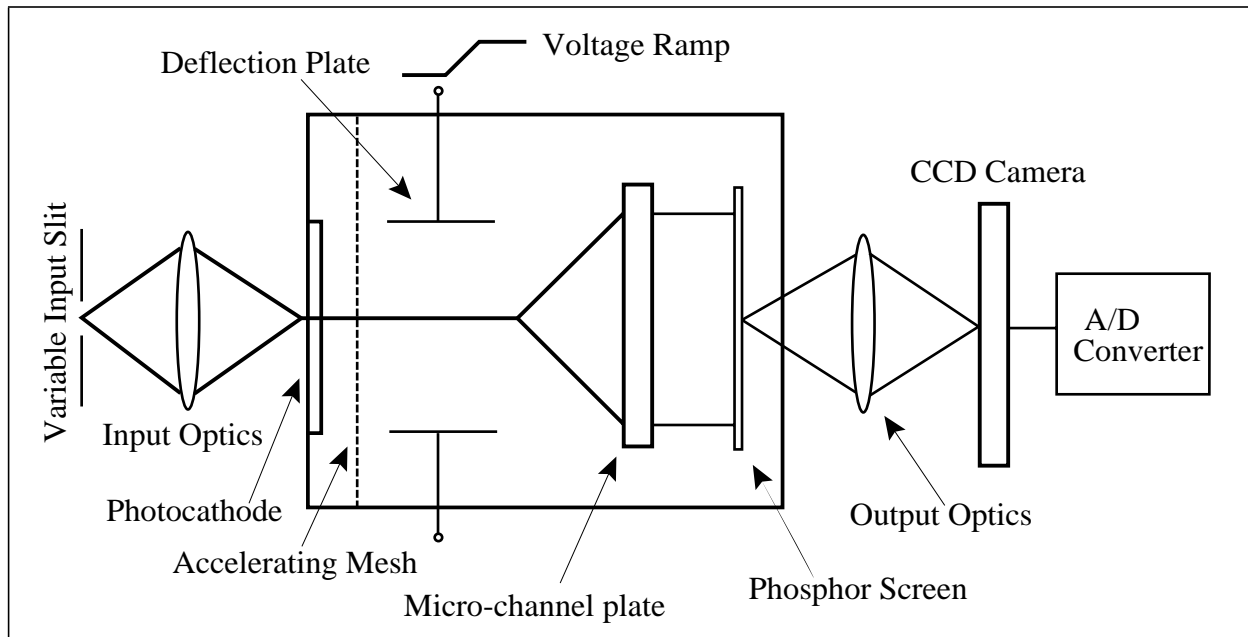
*Envelope frequency*

$$1 \text{ kHz} \sim \gamma_d$$



# Streak Camera

## Layout and Major Specifications

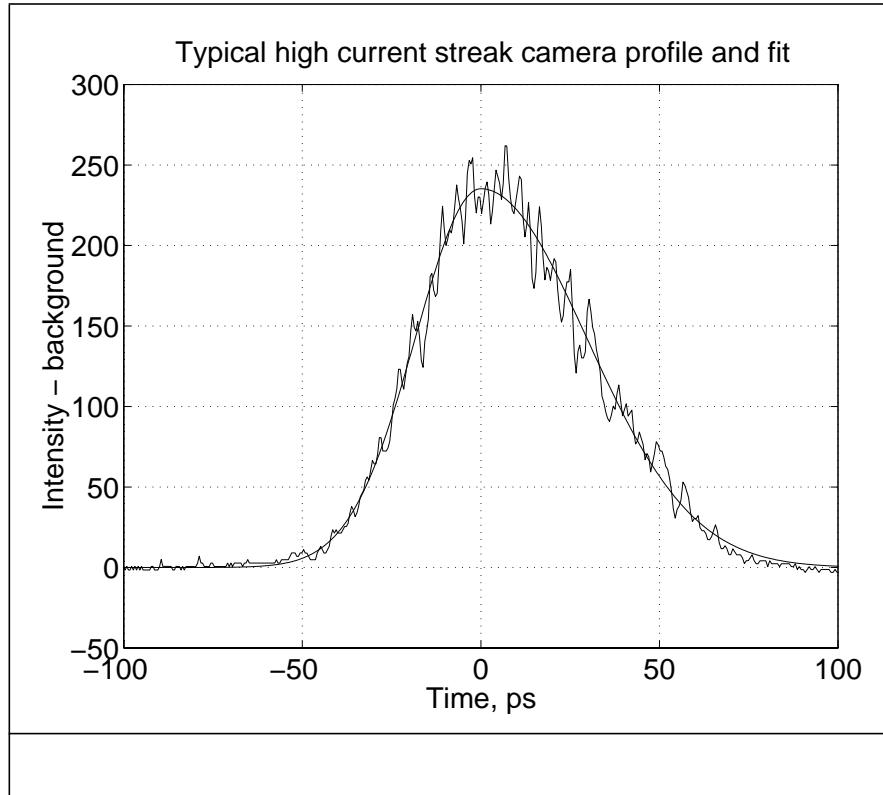


### HAMAMATSU FESCA-500 STREAK CAMERA & CCD SYSTEM

|                   |                  |
|-------------------|------------------|
| Type              | Single Sweep     |
| Time Resolution   | < 700 fs         |
| Spectral Response | 400-800 nm       |
| Streak Rate       | 60-1200 ps/10 mm |
| Trigger Jitter    | < 30 ps          |
| Trigger Rate      | < 1 kHz          |
| CCD # of Pixels   | 1000 by 1018     |
| CCD Readout time  | > 4 s            |

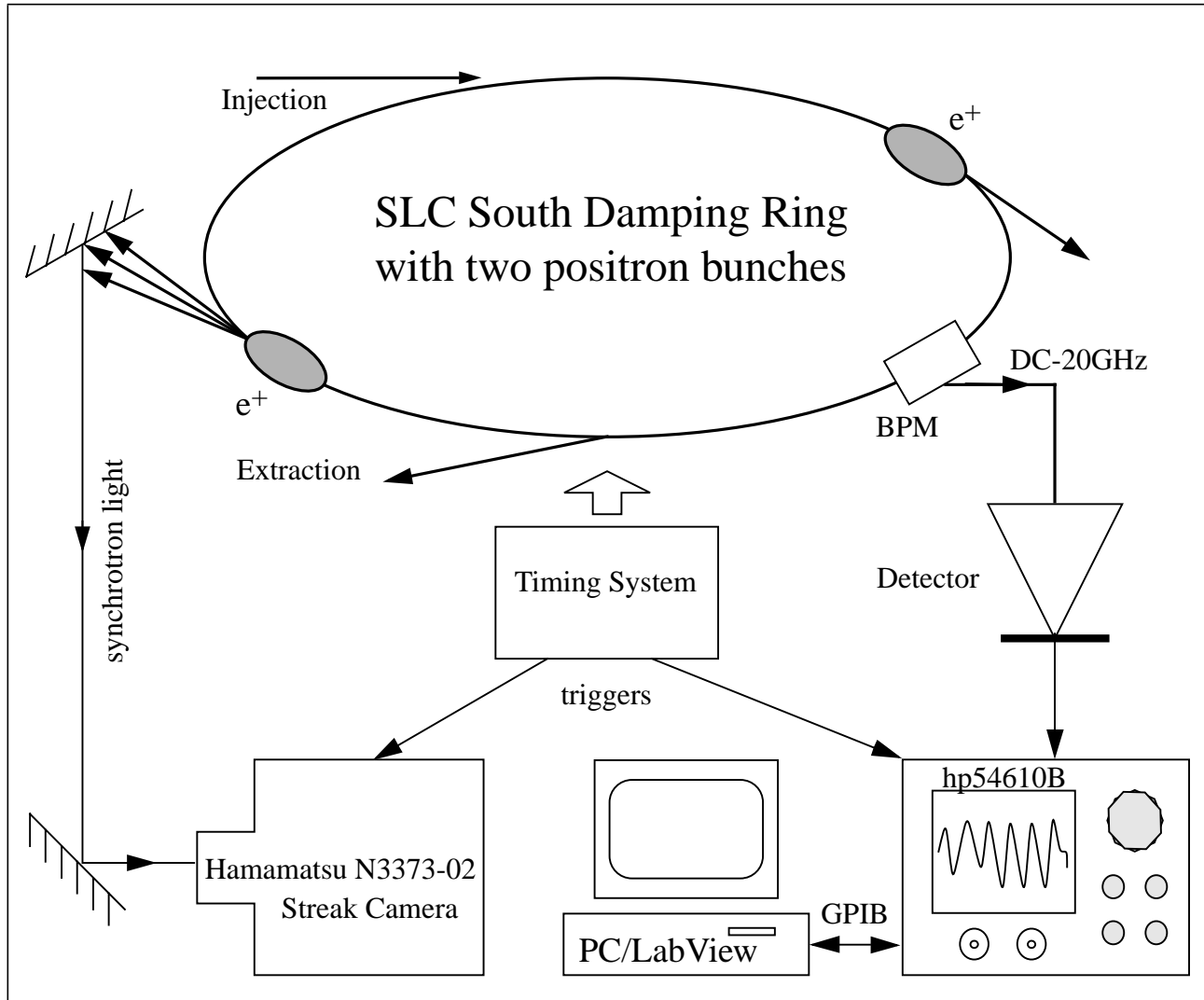
- Advantages: extremely high resolution
- Problems for instability studies: noise, slow data acquisition, trigger jitter, stand-alone instrument...

## Streak Camera Data



- Clear potential well distortion
- Significant amount of noise
- No obvious signs of instability

# Streak Camera Instability Study: Setup

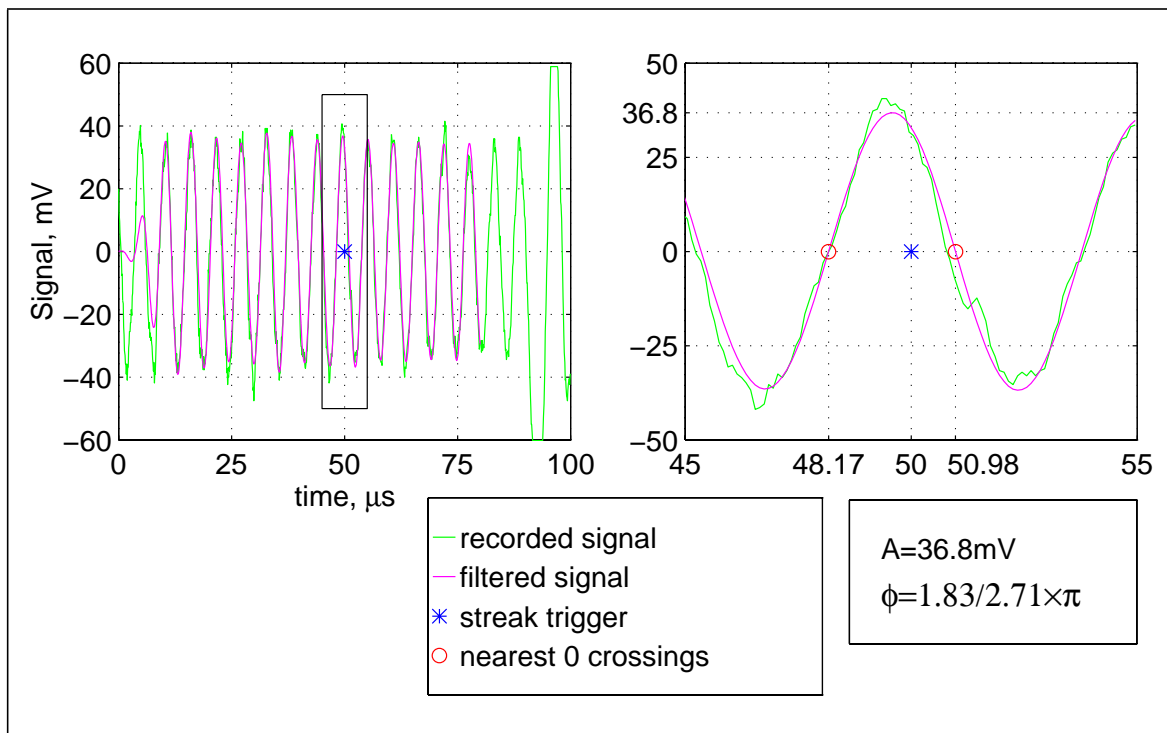


# Streak Camera Instability Study: Data Analysis

## *Scope traces:*

- Digitally filtered to reduce noise
- Used to extract instability amplitude and phase

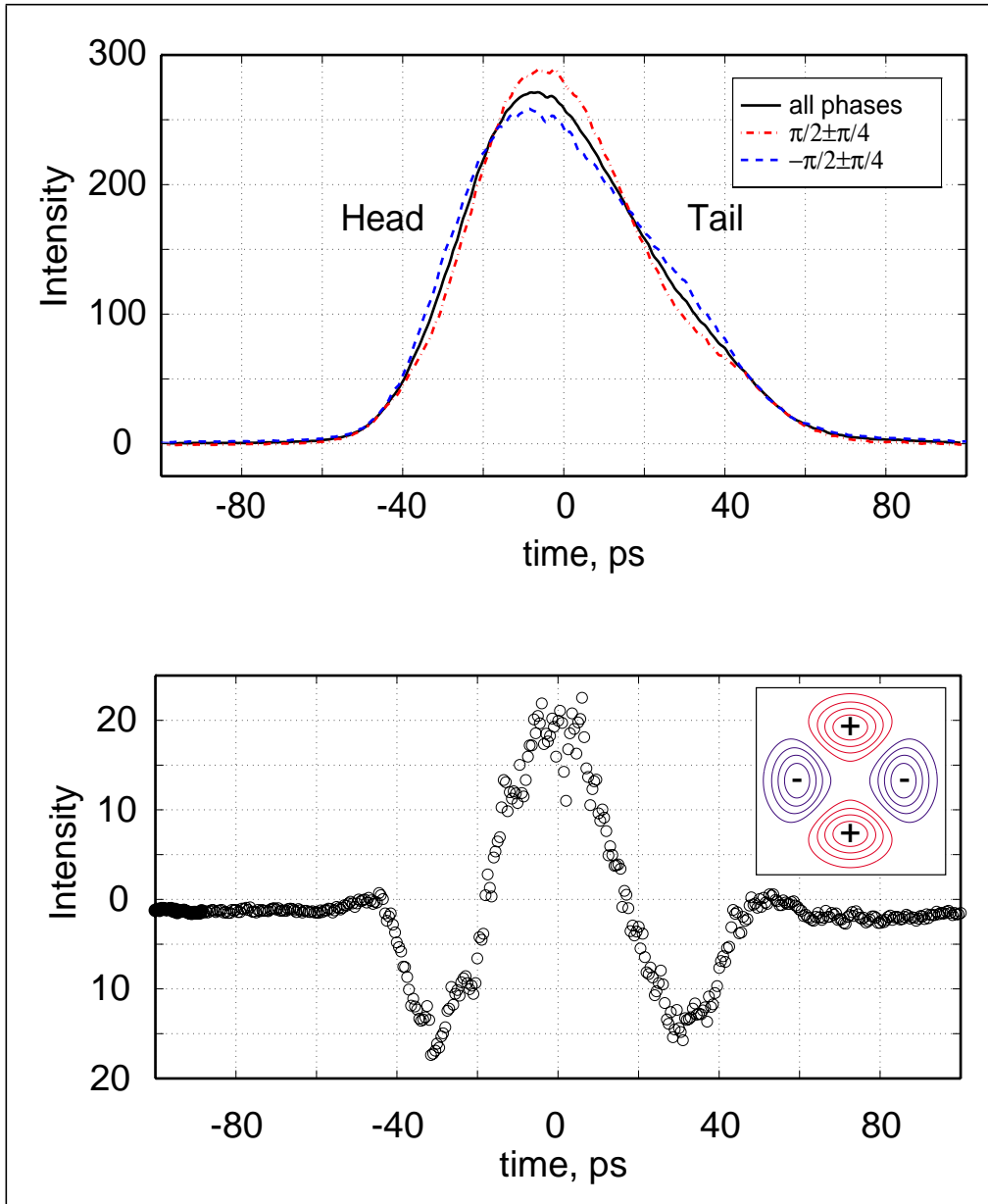
## Extracting “Instability Phase” from Scope Traces



## *Streak profiles:*

- Calibrated for sweep nonlinearity
- Binned in instability amplitude and phase

# Streak Camera Instability Study: Results

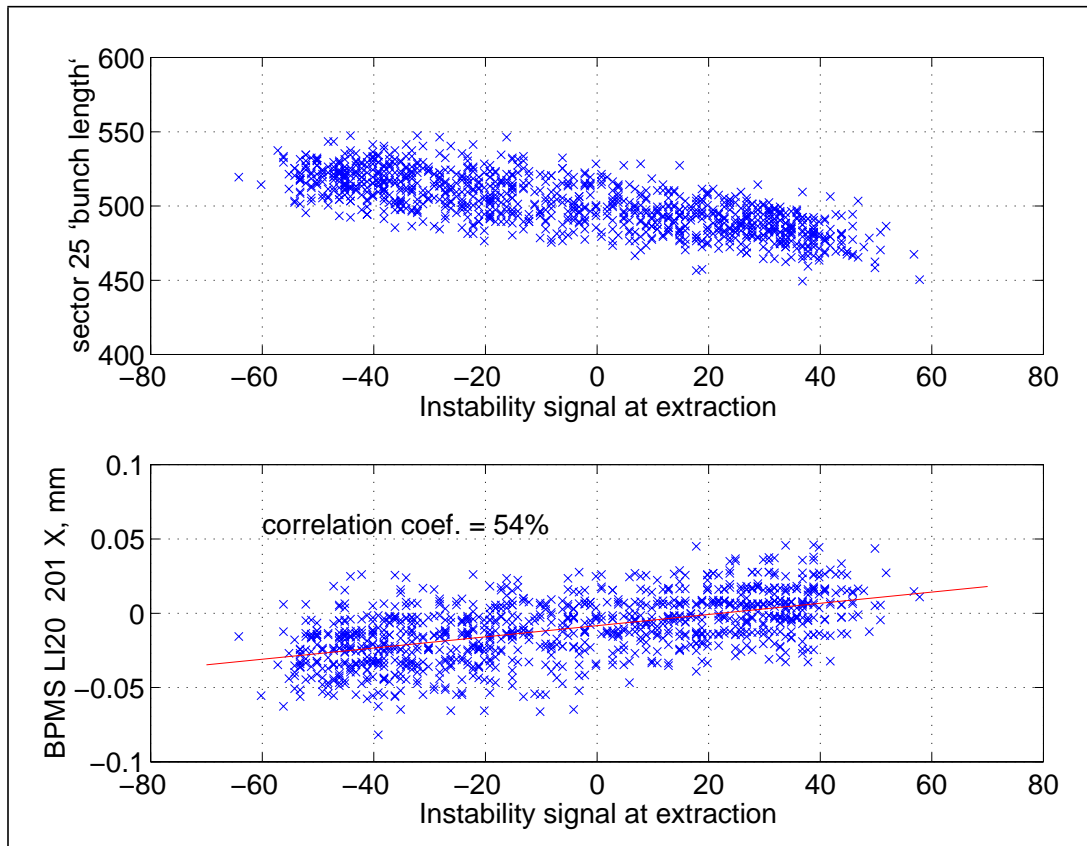


*Unstable mode contains ~3% of beam*



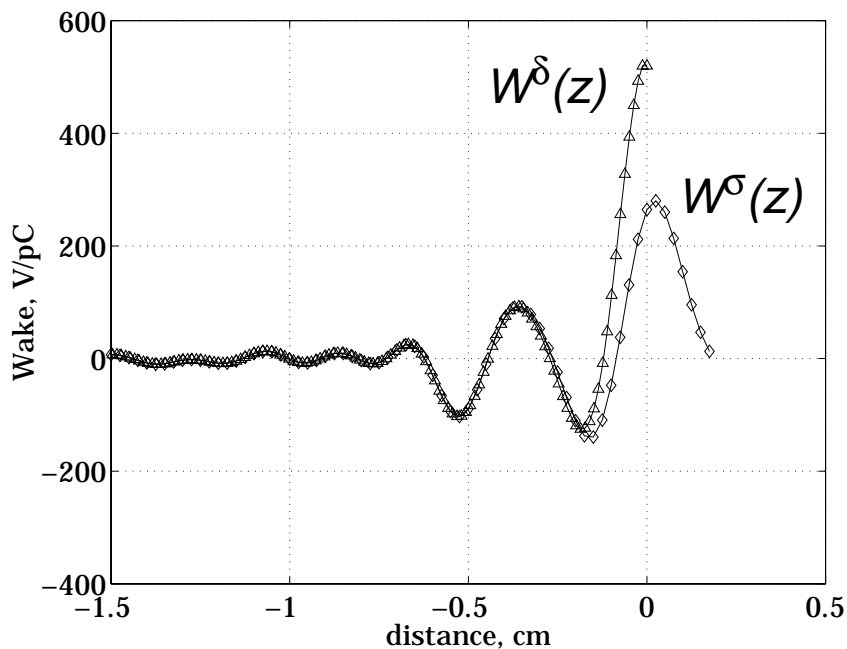
# Linac Correlation Experiment

Correlating Instability Signal at Extraction with Linac Bunch Length and Trajectory



- Instability contributes to the transverse jitter in the linac
- We estimate that about 40% of the jitter power is caused by the instability
- This effect could be a problem for NLC

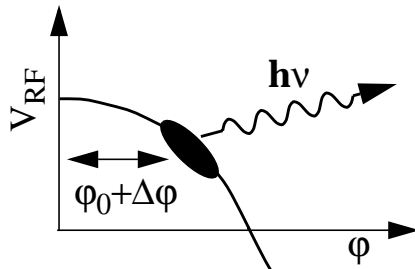
## Bane-Ng Wake Function Model for the SLC Damping Rings



- Calculated using time-domain parts of MAFIA programs
- Used  $\sigma=0.1$  mm driving bunch
- Accounted for all the metallic structures in the chamber
- Hard to model 3D structures were treated approximately

# Synchronous Phase Measurement I

Physics: Losses = Radiation + Wake-Related



$\phi_0$  *synch. phase at  $N \rightarrow 0$*

$\sigma_0$  *bunch length at  $N \rightarrow 0$*

$U_0$  *energy loss/turn due to Synch. Rad.*

$\tilde{\rho}(\omega)$  *Fourier transform of  $\rho(z)$*

- $eV_{RF} \cos(\phi_0 + \Delta\phi) = U_0 + ke^2N$  Energy balance
- $k = -\frac{\Delta\phi}{eN} V_{RF} \sin\phi_0$  Loss factor
- $k = \frac{1}{2\pi} \int \text{Re}(Z(\omega)) |\tilde{\rho}(\omega)|^2 d\omega$  Relation to impedance
- $R = \frac{2\sqrt{\pi}\sigma_0 k}{c}$  Effective resistance

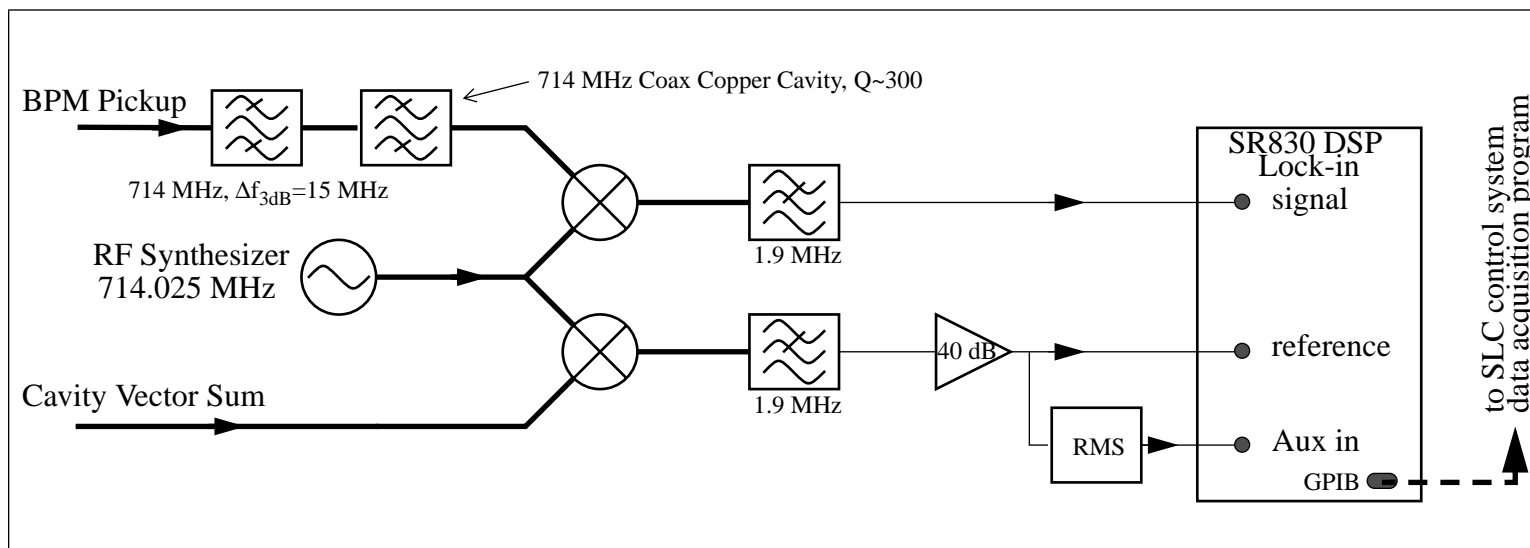
Predictions for SLC Damping Rings based on Bane-Ng model:

- $k \sim 15 \text{ V/pC}$   $R \sim 950 \Omega$  Calculated values
- $\frac{\Delta\phi}{\Delta N} \sim 1.7^\circ \text{ per } 10^{10} \text{ particle loss}$

*Small value, hard to measure*

# Synchronous Phase Measurement II

## New Apparatus



### SR830 Specifications

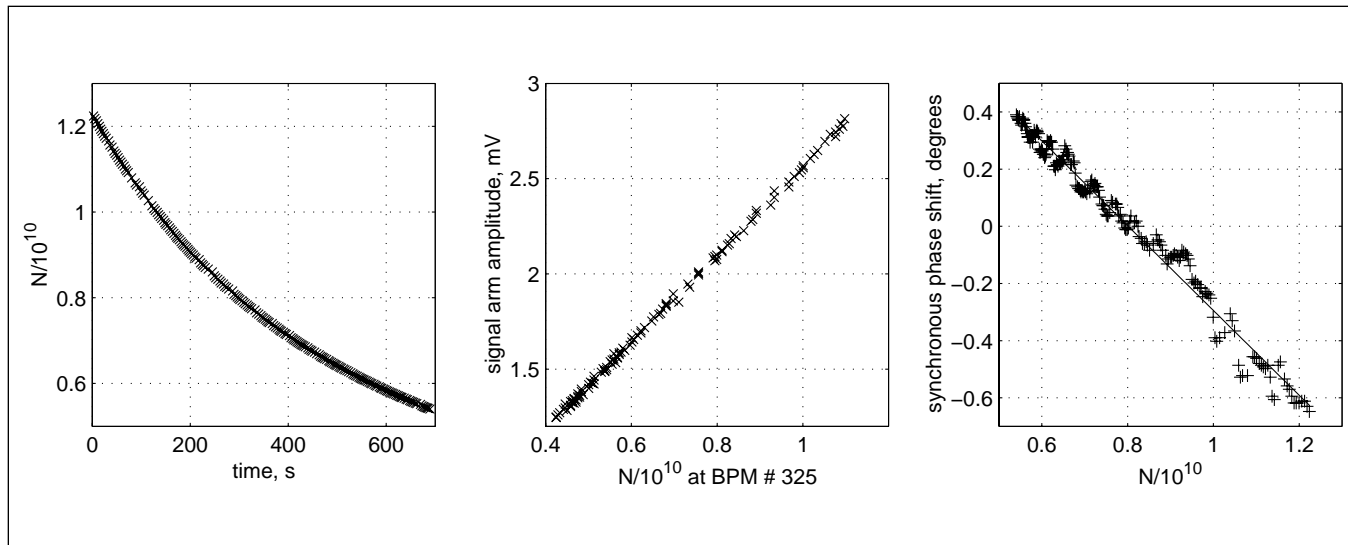
|                  |                          |
|------------------|--------------------------|
| Frequency Range  | 1 mHz to 102 kHz         |
| Rel. Phase Error | $< 0.01^\circ$           |
| Phase Drift      | $< 0.1^\circ/\text{C}$   |
| Time Constants   | 10 $\mu\text{s}$ to 30 s |
| Dynamic Reserve  | $> 100$ dB               |

*Advantages of the apparatus  
over standard vector voltmeters*

- Precision
- Flexibility
- Low cost

# Synchronous Phase Measurement III

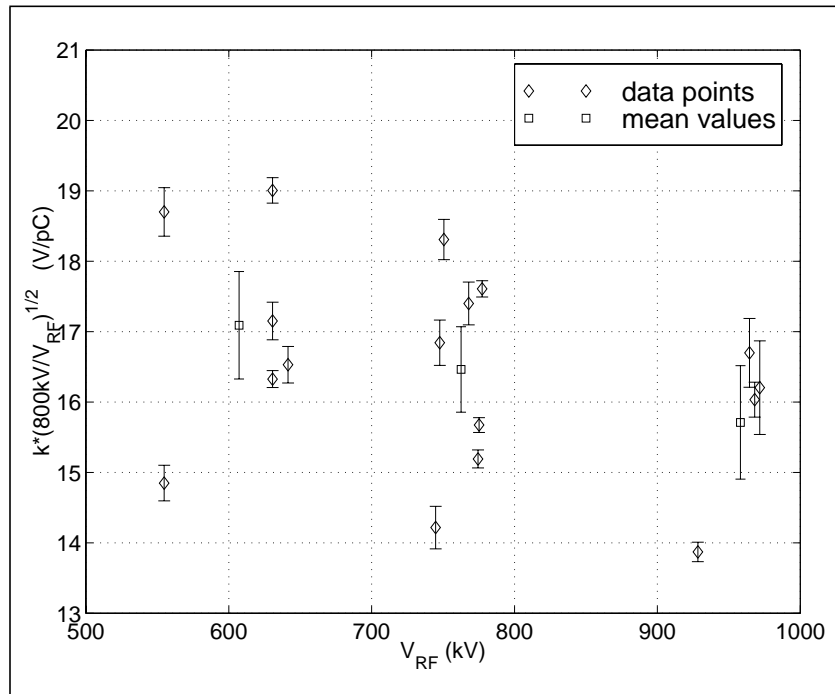
Raw Data for a Typical Store



- Signal is clearly beam induced
- Phase changes linearly with current
- Reproducible from store to store

# Synchronous Phase Measurement IV

## Results

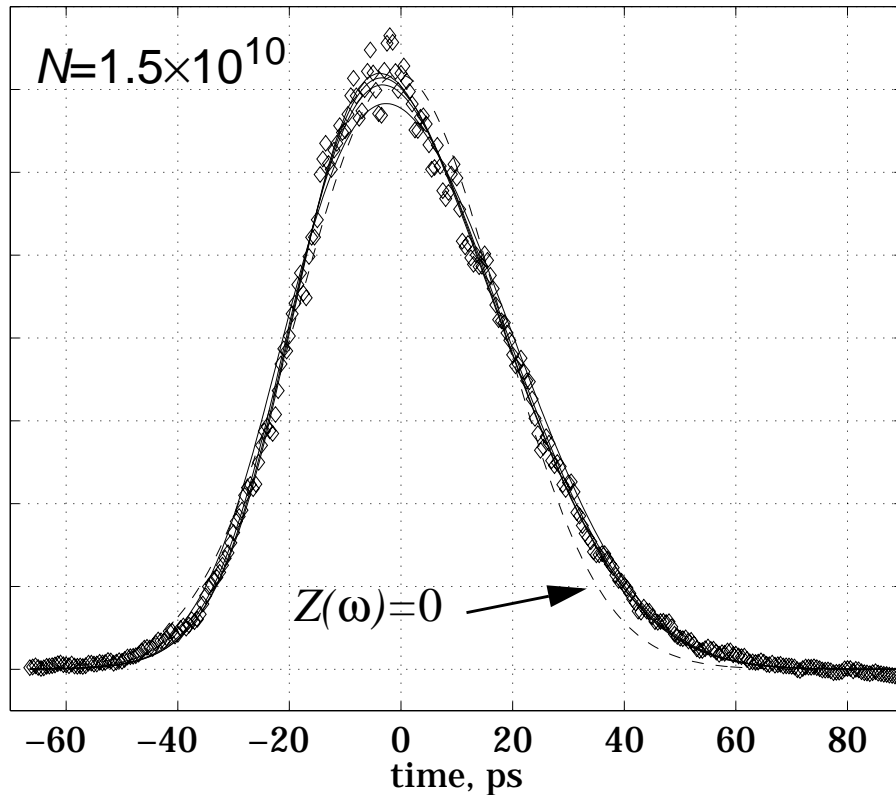


$$k = 16.5 \text{ V/pC} \pm 15\%$$

$$(R \sim 1 \text{ k}\Omega)$$

- Consistent values
- Error mainly due to uncertainty in  $V_{RF}$ ,  $N$
- Good agreement with calculations and streak camera bunch shape measurements at low current.

## Impedance Estimate from Low Current Bunch Shape



- Recorded beam profiles at  $N=9 \times 10^{10}$ - $1.5 \times 10^{10}$
- Fitted them with Haissinski solution for  $Z(\omega)=0$ ,  $Z(\omega)=R$ ,  $Z(\omega)=R-i\omega L$ , and Bane-Ng wake model
- Results:  $R=1 \text{ k}\Omega \pm 130 \text{ }\Omega$ ,  $L \sim \text{few nH}$  (fits poorly)
- Agrees well with Bane-Ng model
- Problems: indirect method, not enough sensitivity



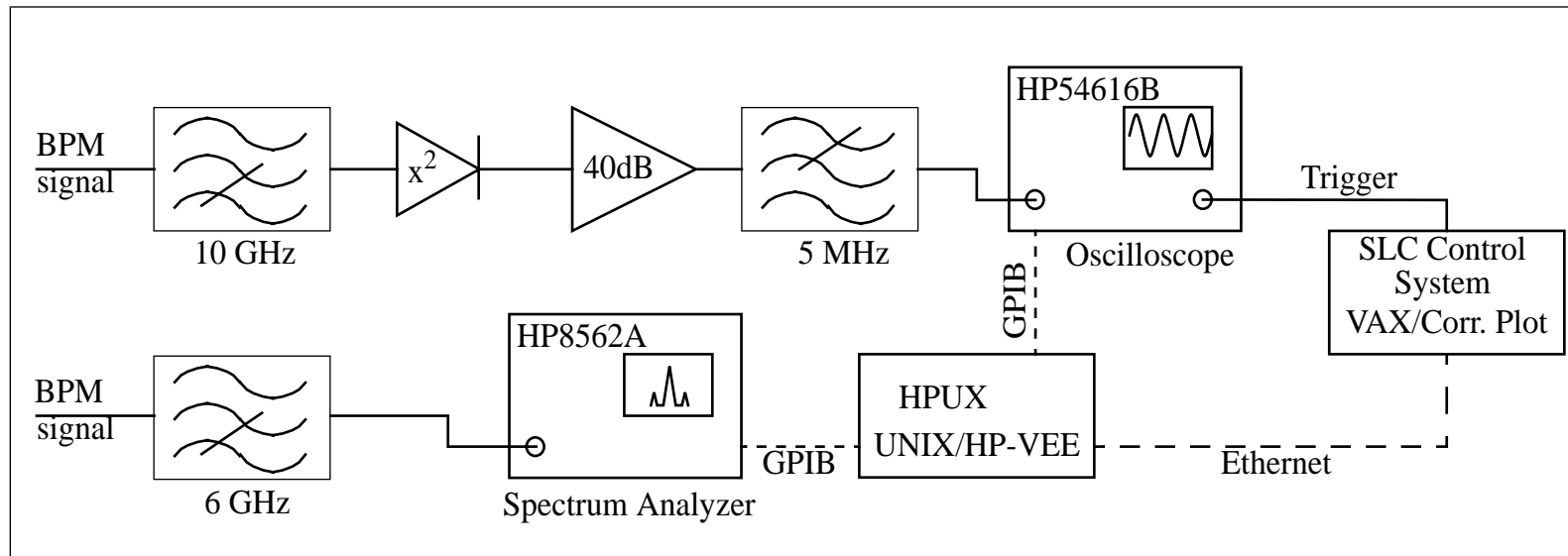
## Summary of Impedance Measurements

- Used three different methods
- Consistent results
- Agreement with Bane-Ng model
- Cannot measure more than 2-3 parameters

*Question: How many impedance parameters do we need to explain high current phenomena?*



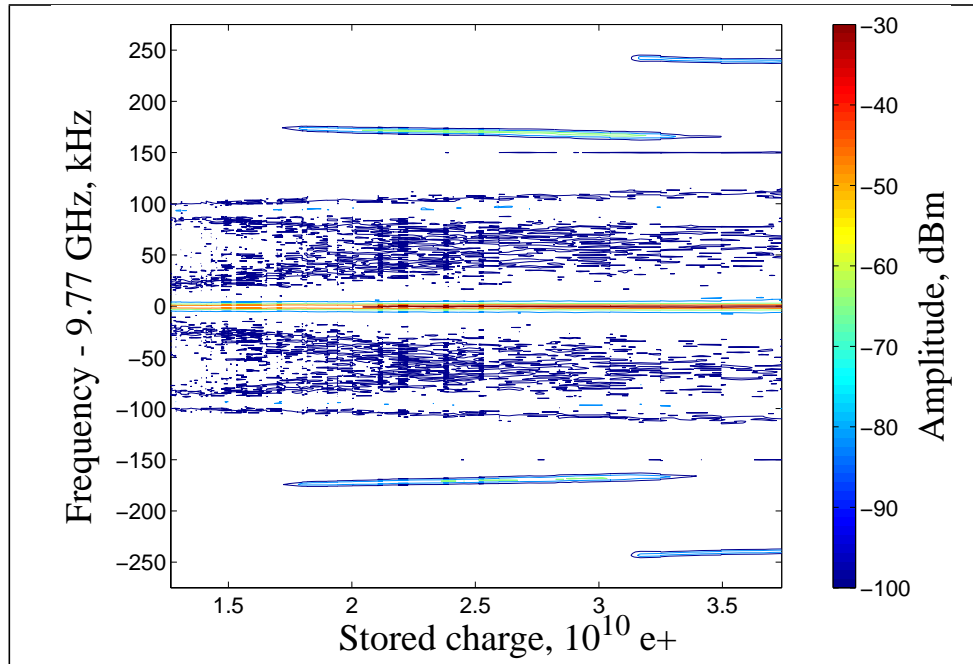
## Stored Beam Experiment: Setup



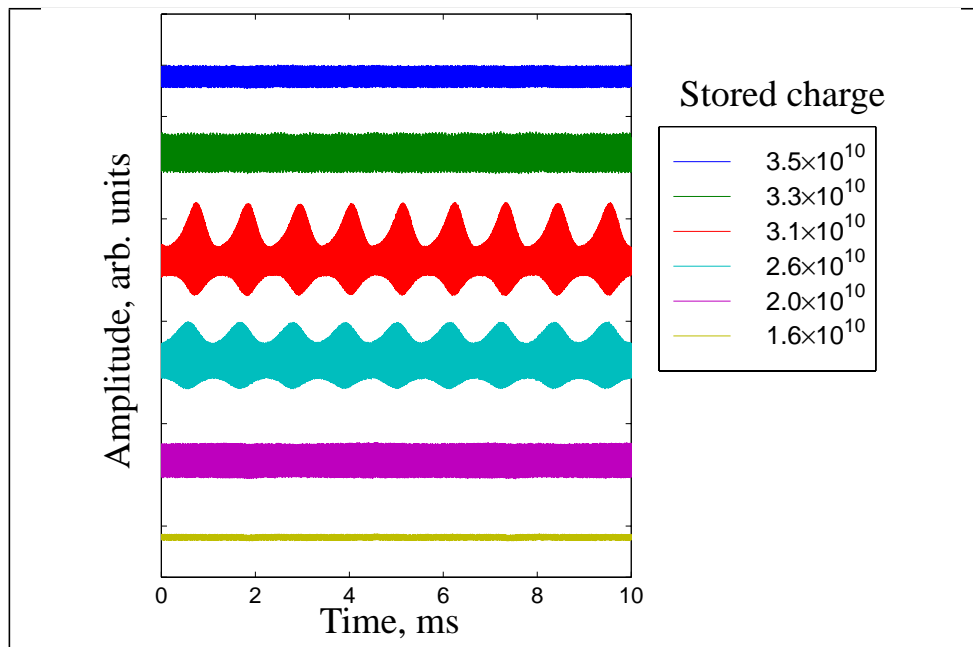
- Positron ring, Single bunch stores ~10 minutes
- Charge decays down from  $\sim 3.5 \times 10^{10}$
- Different RF voltages  $600 \text{ kV} < V_{\text{RF}} < 1 \text{ MV}$
- High frequency BPM signal is measured directly with a spectrum analyzer
- Similar signal from other BPM is demodulated in the detector circuit and measured with an oscilloscope

# Stored Beam Experiment: Data

## Spectrum Analyzer Data

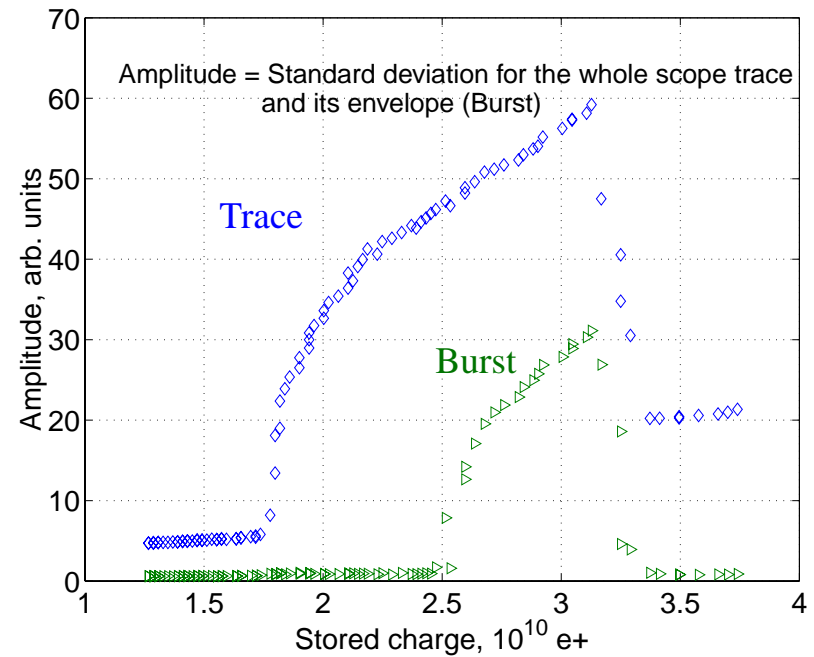
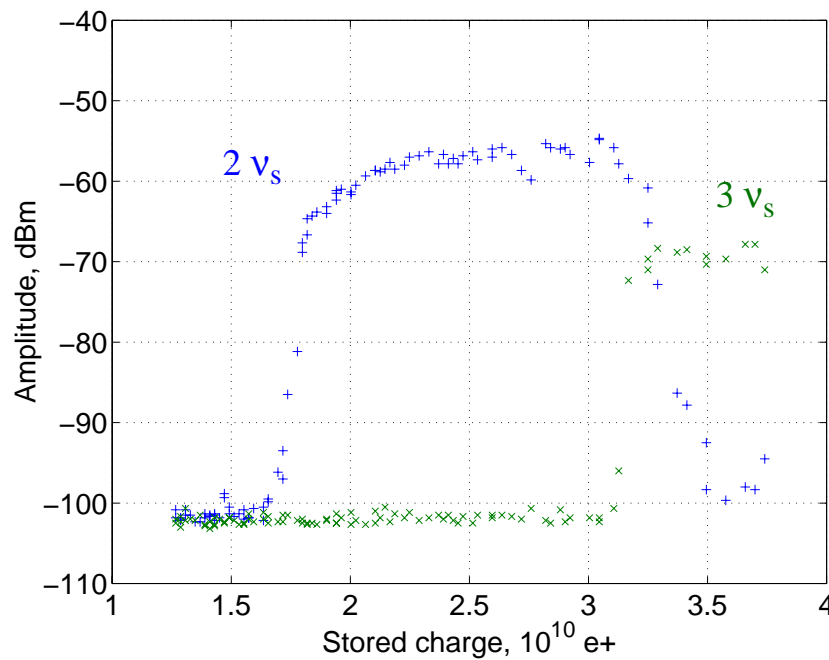


## Scope Traces for Different Stored Charge



# Stored Beam Experiment: Results

Instability Amplitudes from Spectrum Analyzer (left) and Scope Data



- Measurement agreement between two instruments
- Clear thresholds for quadrupole and sextupole modes
- Region of bursting behavior for quadrupole mode
- Quadrupole mode disappears at  $N > 3.3 \times 10^{10}$
- Cannot be explained by azimuthal mode coupling

## Conclusion

- New hardware for instability diagnostics ✓
- Measured properties of instability ✓
  - Phase space structure
  - Effect on the linac
  - Driven and self-excited beam response
- Impedance-related measurements ✓
  - Agreement between different experiments
  - Agreement with calculated model
- Theoretical explanation ✓?